



# *High frequency electromagnetic field irradiation*

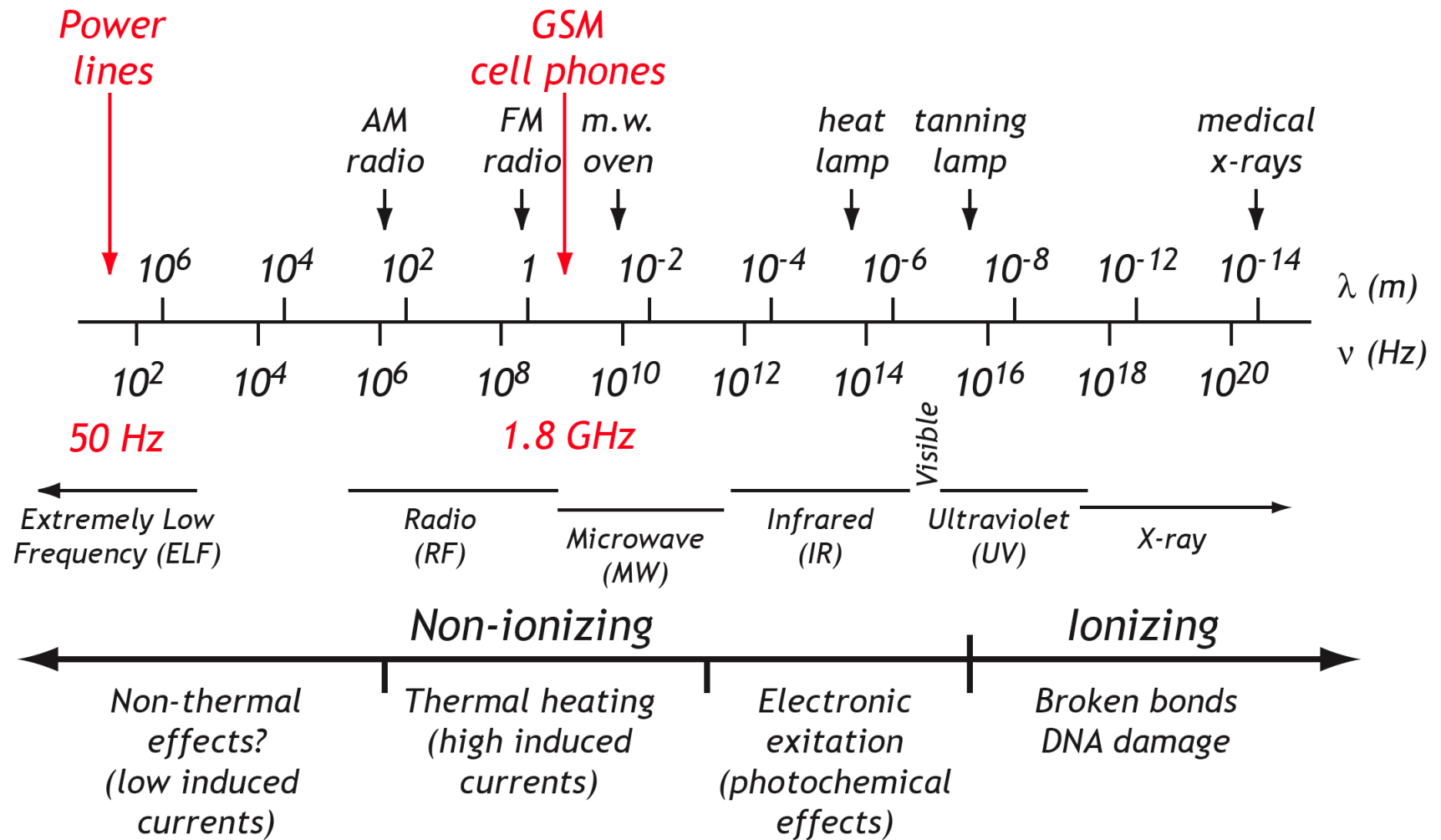
*Andrea Contin*

*2005*

# Outline

- *GSM signal*
- *e.m. waves*
- *resonant cavities*
- *ETHZ apparatus*
- *SAR analysis*

# e.m. spectrum



# High frequency irradiation

*High frequency e.m. waves hardly penetrate inside the body, largely because of the water content of the tissues:*

$$I = I_0 e^{-d/L}, \quad L < \lambda / 10$$

<i>frequency</i>	<i><math>\lambda</math> (m)</i>	<i>L (m)</i>
<i>50 Hz</i>	<i>6000000</i>	<i>600000</i>
<i>1 kHz</i>	<i>300000</i>	<i>30000</i>
<i>1 MHz</i>	<i>300</i>	<i>30</i>
<i>1 GHz</i>	<i>0,3</i>	<i>0,03</i>

# *Specific Absorption Rate (SAR)*

*The energy absorbed by the body is normalized to weight and time, and measured as SAR (Specific Absorption Rate), in units of:*

$$\left[ \frac{\text{W}}{\text{kg}} \right] = \left[ \frac{\text{J}}{\text{kg s}} \right] = \left[ \frac{\text{Energy}}{\text{kg s}} \right]$$

# High frequency irradiation: requirements

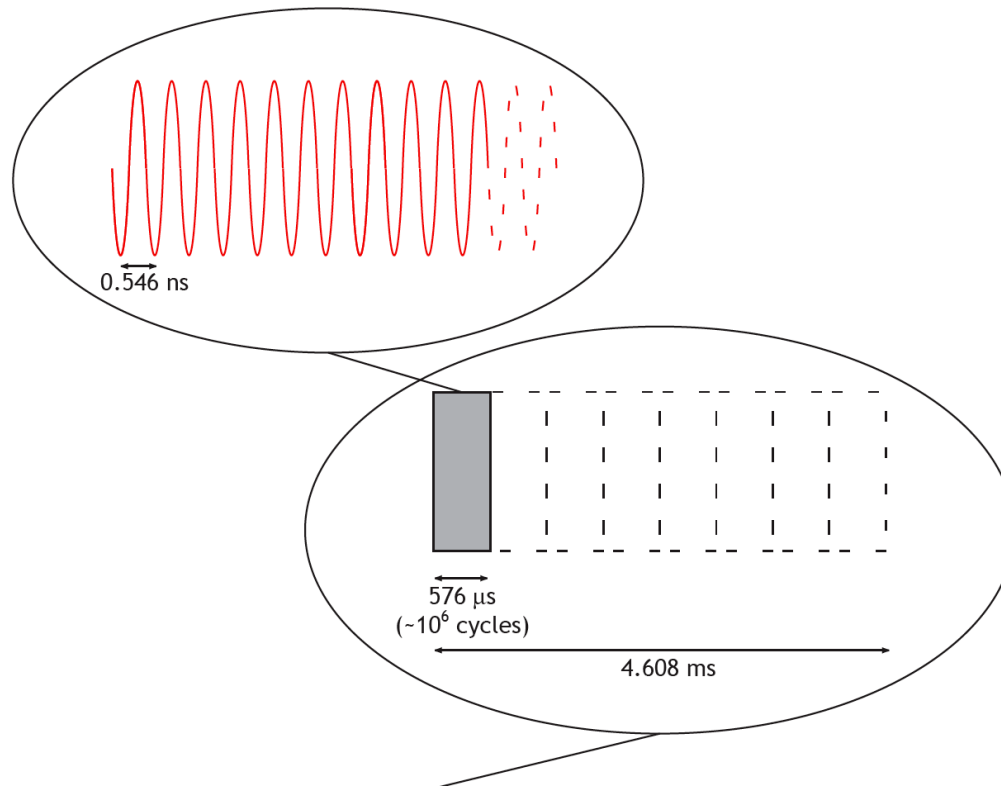
- GSM signal (i.e. flexible signal)
- Fit into commercial incubator
- Standard Petri dishes
- Monolayer cells (in suspension if with limited water content)
- Temperature rise negligible at average SAR=2W/kg
- No temperature hot spots
- Peak SAR > 50 W/kg/ $W_{input}$  (note: 2 W/kg average = 150 W/kg peak in DTX mode)
- SAR nonuniformity < 30%
- SAR uncertainty < SAR nonuniformity
- Isolation between exposure and sham < 30dB
- Same exposure and sham conditions with continuous monitoring
- Self-detecting malfunctioning
- Stable power (feedback regulation of the output power of the RF generator)
- ...

*resonant cavity*

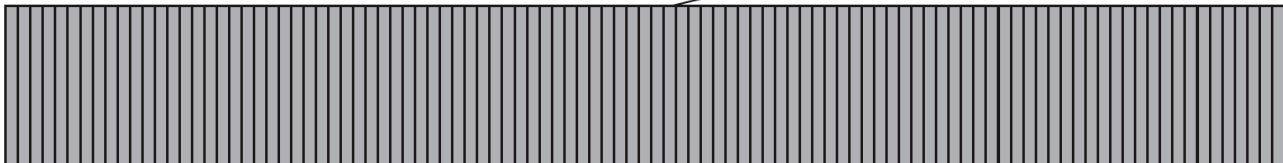
# *GSM transmission - 1800 MHz band*

- *bandwidth: 75 MHz*
- *number of 200 kHz channels: 374*
- *number of phones which can use the same channel: 8 (with Time Division Multiple Access - TDMA)*
- *pulse duration: 4.608 ms*
- *active time in one pulse: 576  $\mu$ s (pulse modulation: 217 Hz)*
- *omitted pulses: 1 every 26 (additional pulse modulation: 8.34 Hz)*
- *power emission is adjusted to the strength of the signal: Adaptive Power Control (APC)*
- *power is switched off if not speaking: Discontinuous Transmission (DTX)*

# GSM signals

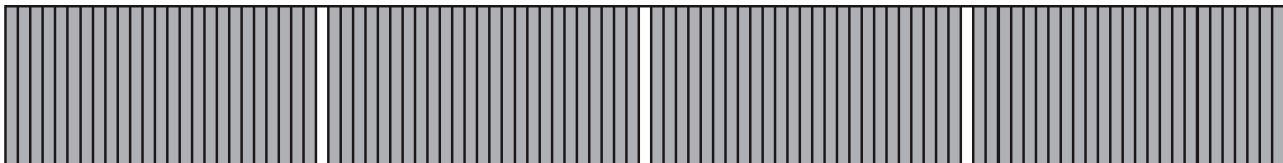


GSM 217Hz



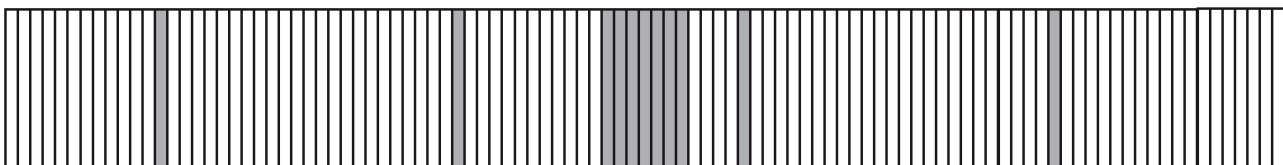
*Peak/average SAR = 8*

GSM Basic  
(send)



*Peak/average SAR = 8.3*

GSM DTX  
(receive)



*Peak/average SAR = 69.3*



# GSM handsets

- maximum power allowed by law: 1 W
- fields at 2.2 cm from antenna:  $E=200$  V/m,  $B=6$   $\mu$ T
- intensity at 2.2 cm from antenna:  $I=200$  W/m<sup>2</sup> (1/4 of the Sun's radiation in a clear day)
- max SAR: 20-25 W/kg

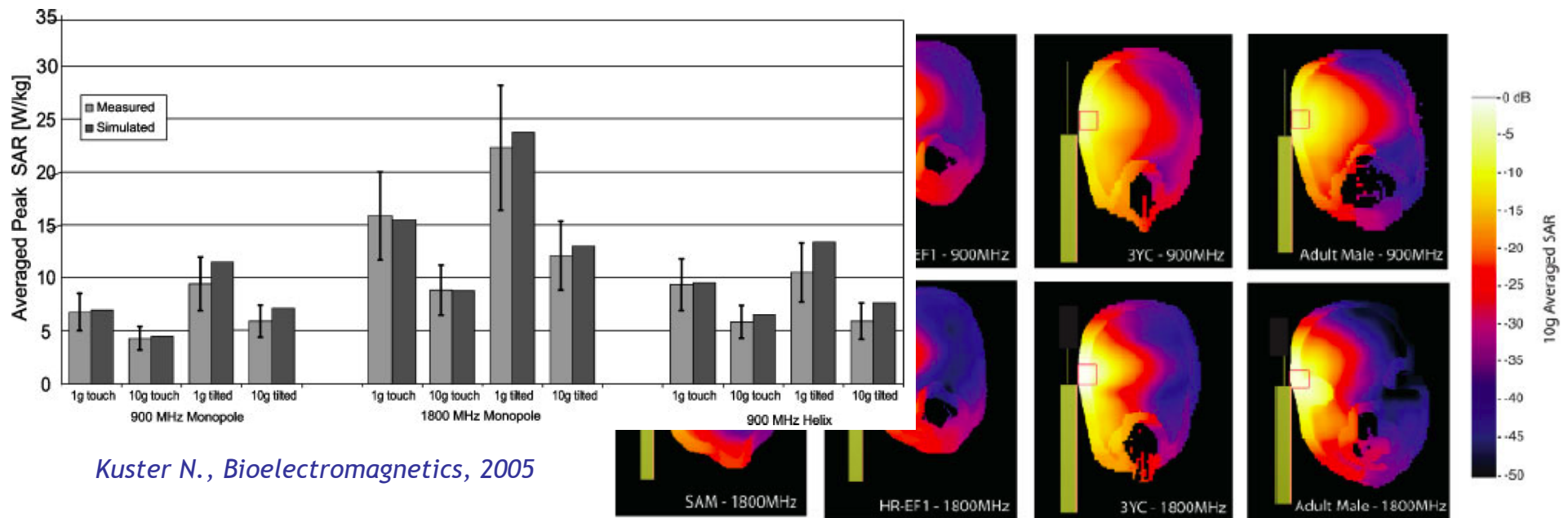


Fig. 7. Ten-gram average SAR distributions for SAM and the three anatomical phantoms in the "tilted" position for the GMP with monopole antenna. 0 dB corresponds to 15 W/kg normalized to 1W antenna output power. The square indicates the location of the averaged SAR maximum.

# GSM antennas

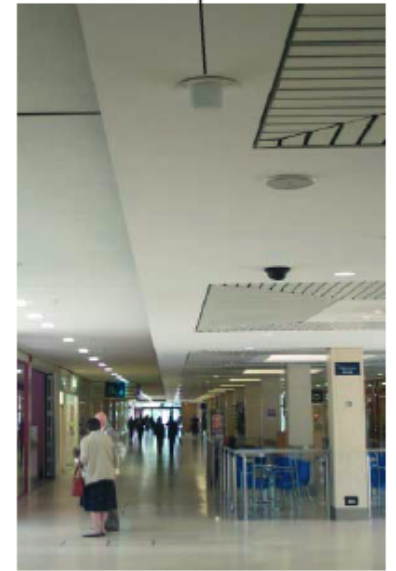
- *standard cell typical power: 3 kW (directional, 120° sector)*
- *beam vertical aperture: 6°*
- *maximum intensity at 50 m from antenna:  $I=100 \text{ mW/m}^2$  (1000 times smaller than from handset)*



*standard cell*



*microcell*



*picocell*

# Waveguide

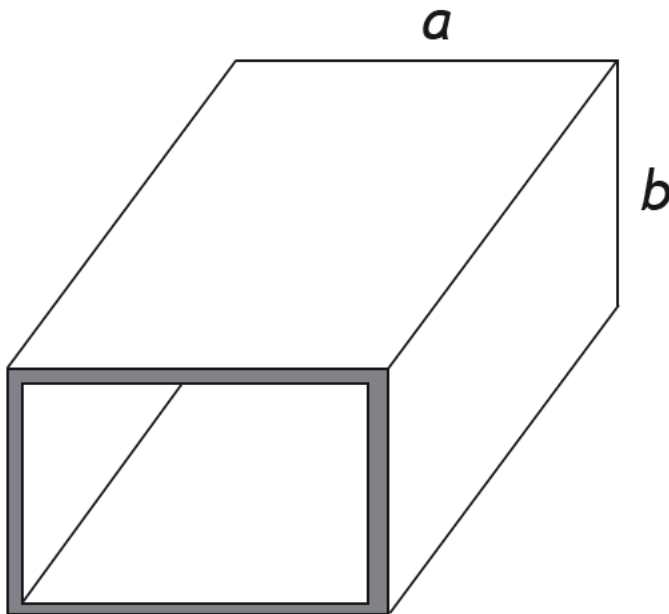
*A wave guide is an empty tube with conductive walls into which an electromagnetic wave propagates.*

*It is used when a high frequency signal ( $>1\text{GHz}$ ) has to be transmitted for long distances without power losses.*

*A waveguide can be imagined as an extension of the coaxial cable (e.g., TV cable).*

# Waveguide

(infinite length box with conductive walls)



## Consequences of conductive walls:

*the electric field can only be perpendicular to the walls*

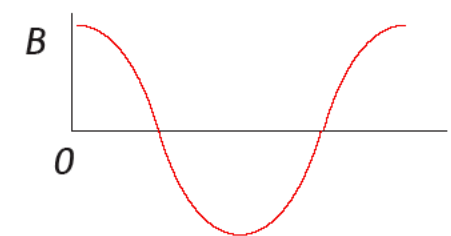
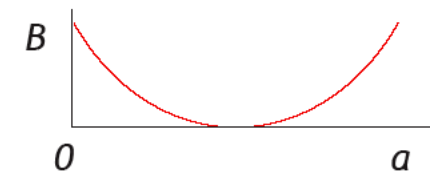
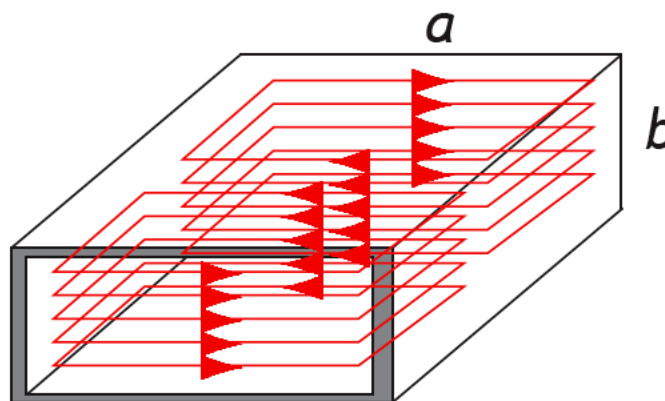
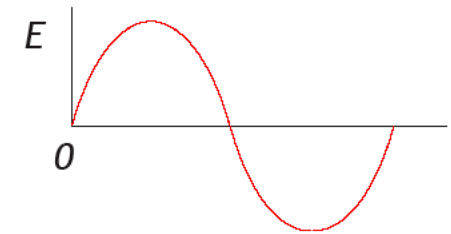
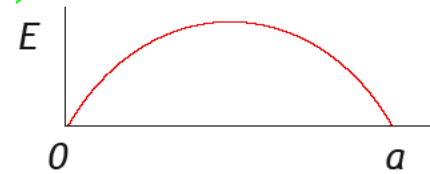
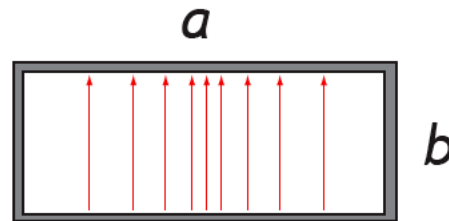
*the magnetic field can only form close loops parallel to the walls and perpendicular to the electric field*

*an e.m. wave travelling inside the cavity can be a superposition of several waves with different wavelength, phase and amplitude*

*the e.m. wave travelling inside the cavity is “reflected” at the walls*

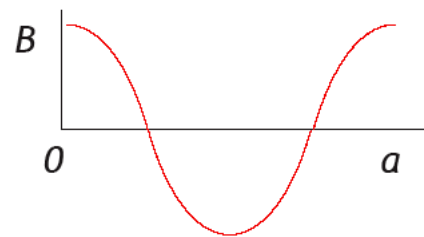
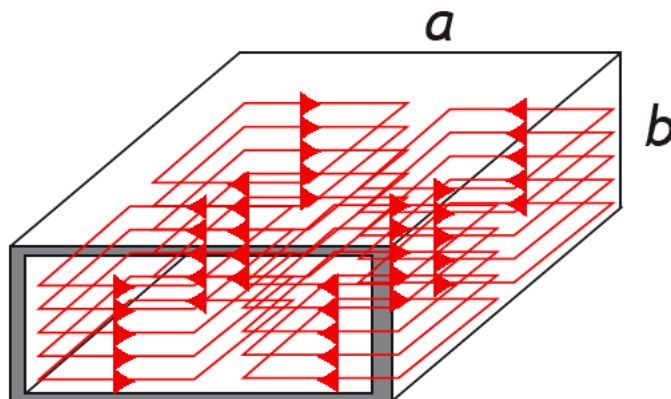
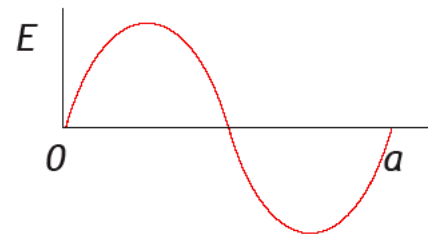
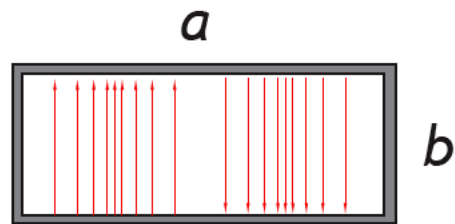
# Electric and Magnetic fields inside the waveguide

(dominant mode)



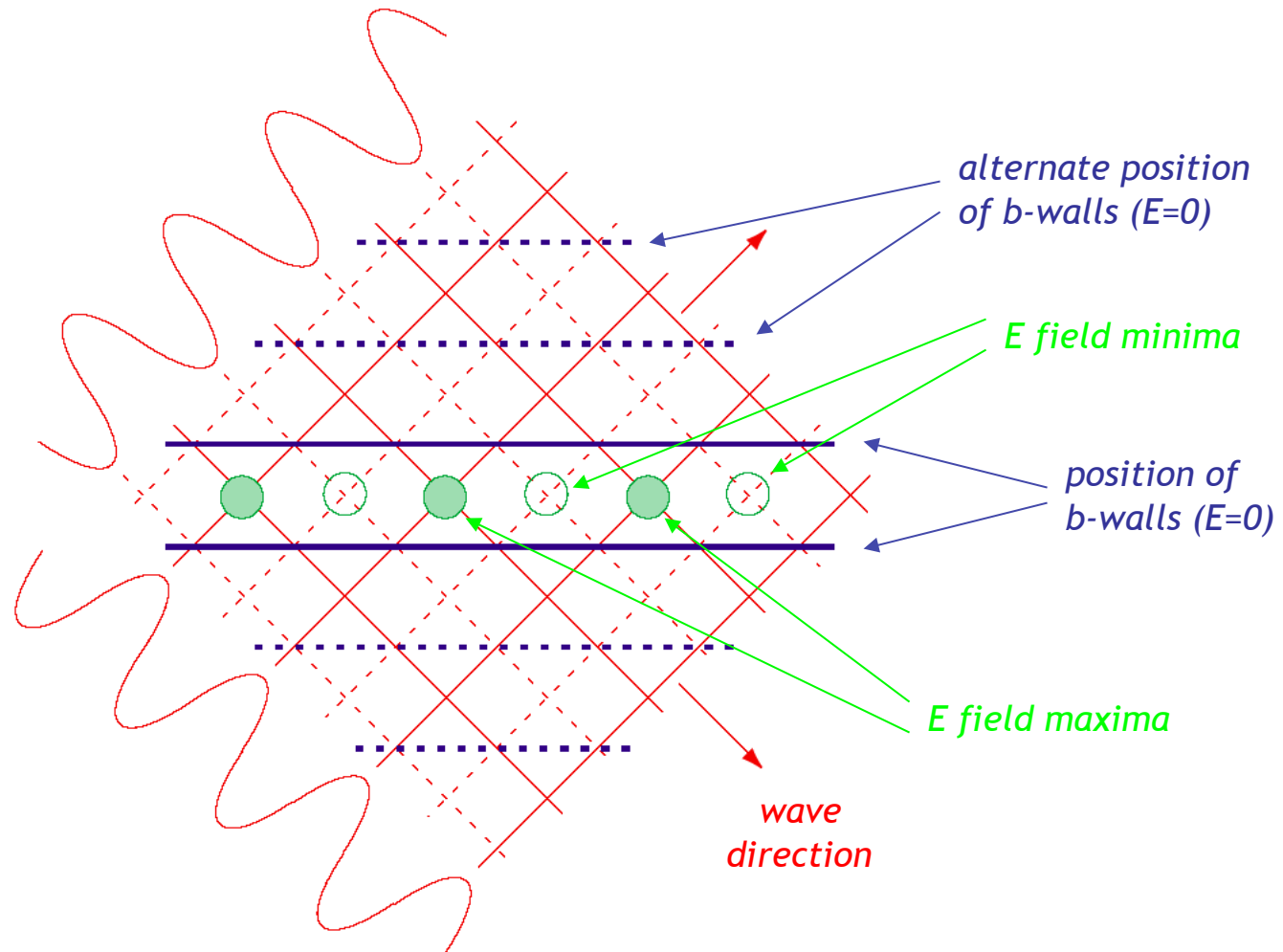
# *Electric and Magnetic fields inside the waveguide*

*(other modes)*



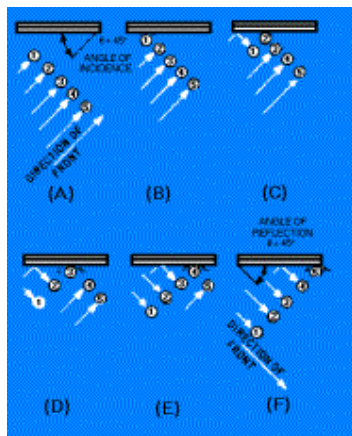
# How to get $E=0$ at b-walls

*two waves with the same frequency  
moving at an angle from each other*

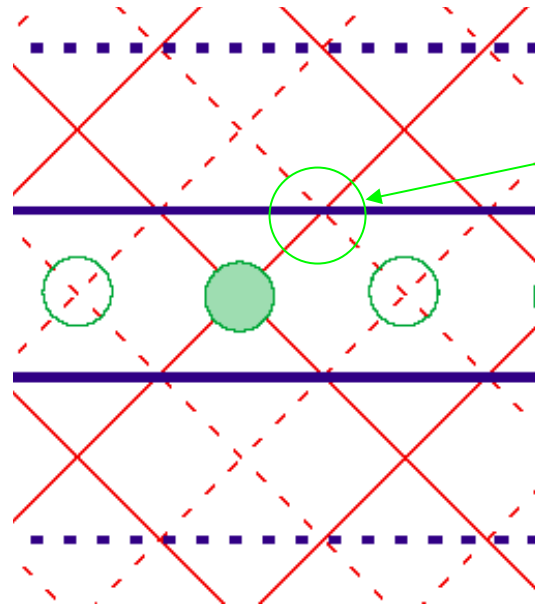


# Reflection on the walls

Reflection:



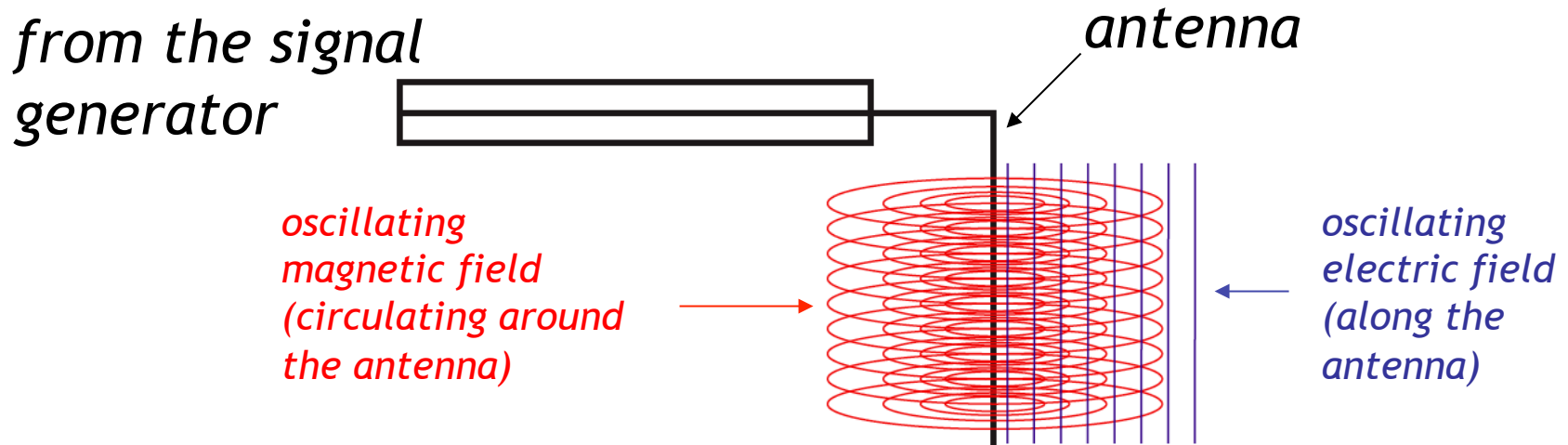
*A reflection changes the phase of the wave by  $180^\circ$*



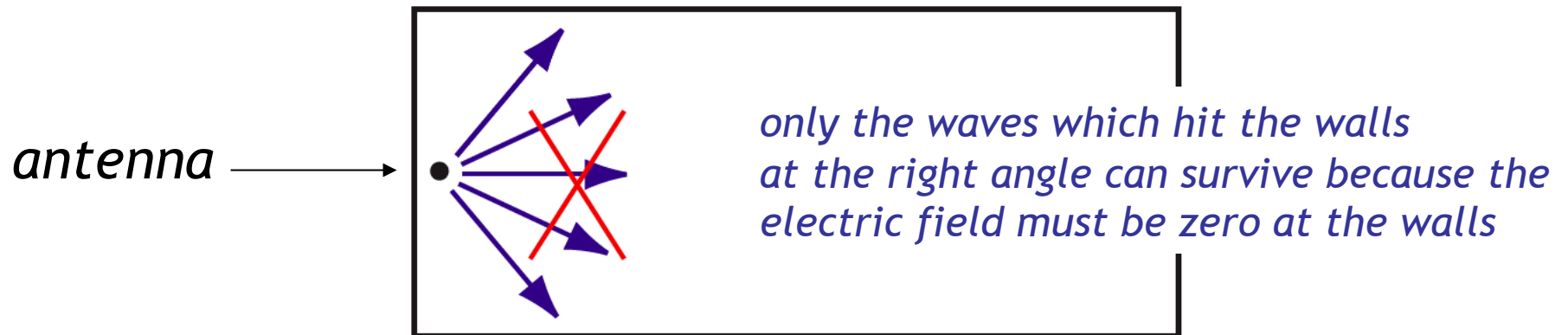
*The incident wave has the  $E$  field at its minimum; the reflected wave at its maximum*



# How the resonant wave is induced in the waveguide

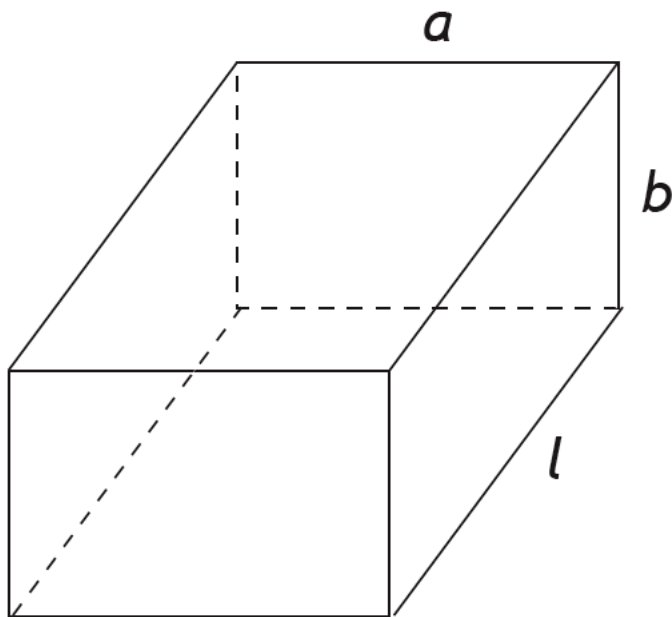


*both the magnetic and the electric field propagate in space*



# *Resonant cavity*

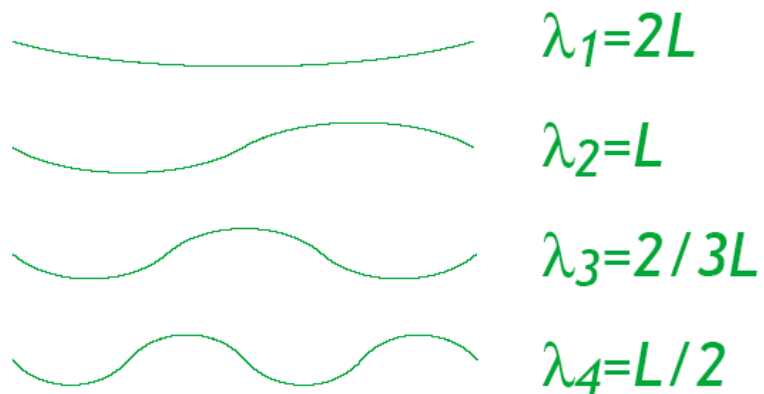
*(finite length box with conductive walls)*



*effect of conductive walls:*

*same as waveguide*  
*(but two more boundary conditions)*

## Rope fixed on both ends



$$\lambda = \frac{2L}{n}$$

$$k = \frac{2\pi}{\lambda} = \frac{n\pi}{L}$$

*all waves (armonics) can be present at any time*

*a perturbation travelling along the rope is a superposition of all armonics with different phases and amplitudes*

*a perturbation travelling along the rope is “reflected” at the fixture*

## *Resonant cavity: electric field configuration*

$$\bar{E} = \bar{E}_0 \cos(\omega t - \bar{k} \cdot \bar{r})$$

$$k_1 = \frac{n_a \pi}{a}; k_2 = \frac{n_b \pi}{b}; k_3 = \frac{n_l \pi}{l}$$

← *boundary conditions*

$$E_x = E_1 \cos(k_1 x) \sin(k_2 y) \sin(k_3 z) \cos(\omega t)$$

$$E_y = E_2 \sin(k_1 x) \cos(k_2 y) \sin(k_3 z) \cos(\omega t)$$

$$E_z = E_3 \sin(k_1 x) \sin(k_2 y) \cos(k_3 z) \cos(\omega t)$$

## *E.M. frequency*

$$\nu = \frac{\omega}{2\pi} = \frac{kc}{2\pi} = \frac{c}{2\pi} \sqrt{\frac{n_a^2}{a^2} + \frac{n_b^2}{b^2} + \frac{n_l^2}{l^2}}$$

*If the electric field is vertical (along b dimension):*

$$n_b = 0$$

$$\nu = \frac{c}{2\pi} \sqrt{\frac{n_a^2}{a^2} + \frac{n_l^2}{l^2}}$$

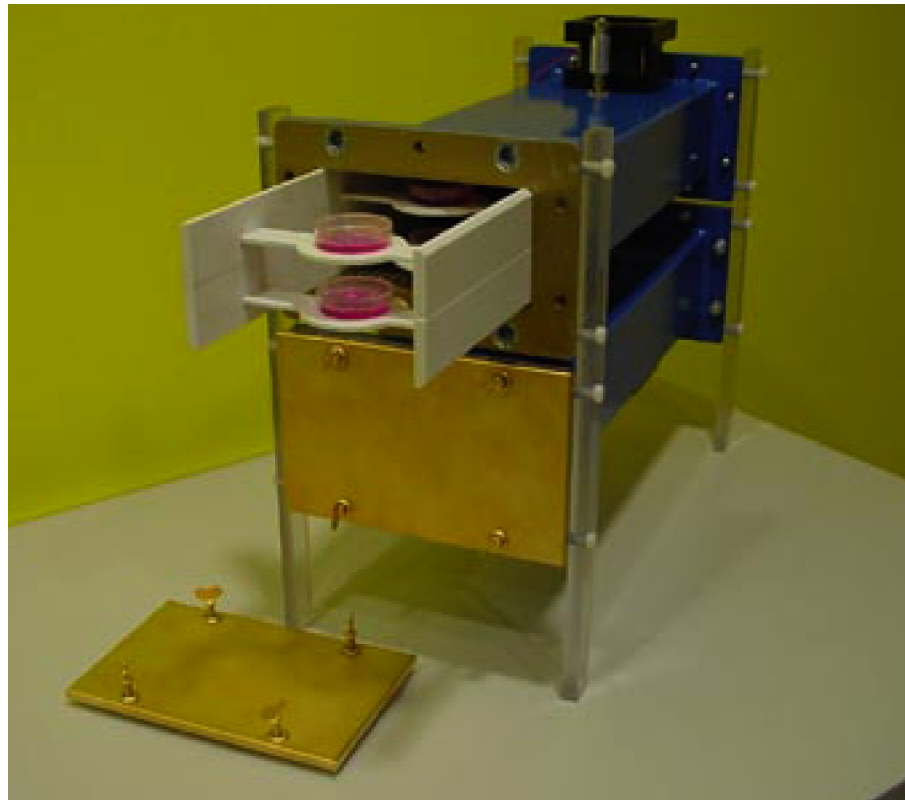
$$|E| = E_y = E_2 \sin(k_1 x) \sin(k_3 z) \cos(\omega t)$$

then, from :  $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ ,  
B can be derived :

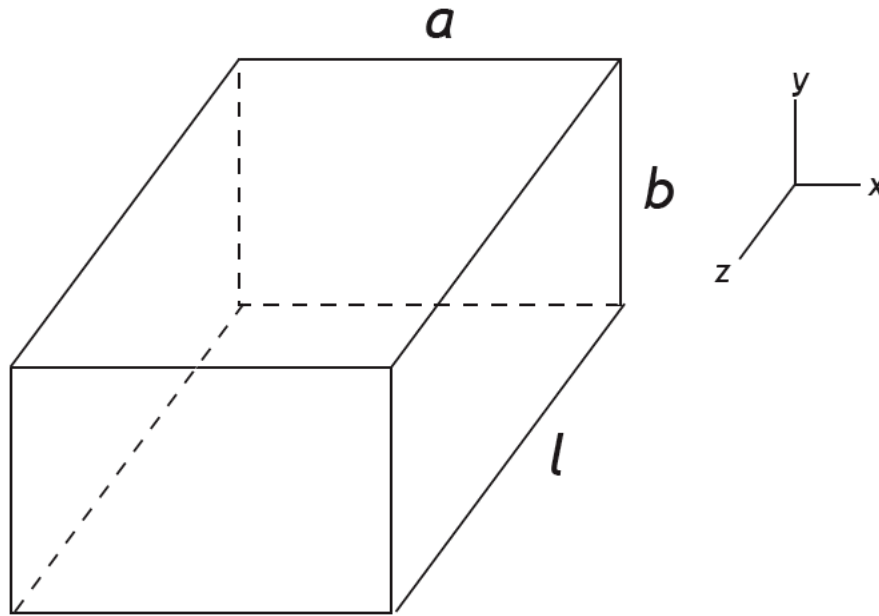
$$B_x = \sin(k_3 z) \cos(k_1 x)$$

$$B_z = -\cos(k_3 z) \sin(k_1 x)$$

# *ETHZ Apparatus*



# ETHZ Apparatus

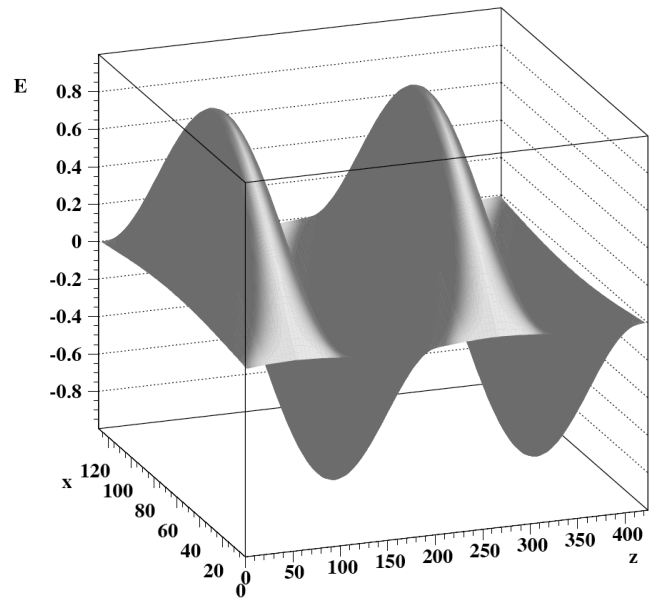


$a=129.6 \text{ mm}$   
 $b=64.8 \text{ mm}$   
 $l=425 \text{ mm}$

na	nb	nl	frequency (GHz)
1	0	1	1.209
2	0	1	2.340
3	0	1	3.488
1	0	2	1.355
2	0	2	2.418
3	0	2	3.541
1	0	3	1.568
2	0	3	2.544
3	0	3	3.628
1	0	4	1.824
2	0	4	2.710
3	0	4	3.746
1	0	5	2.109
2	0	5	2.909
3	0	5	3.892
1	0	6	2.412
2	0	6	3.135
3	0	6	4.064

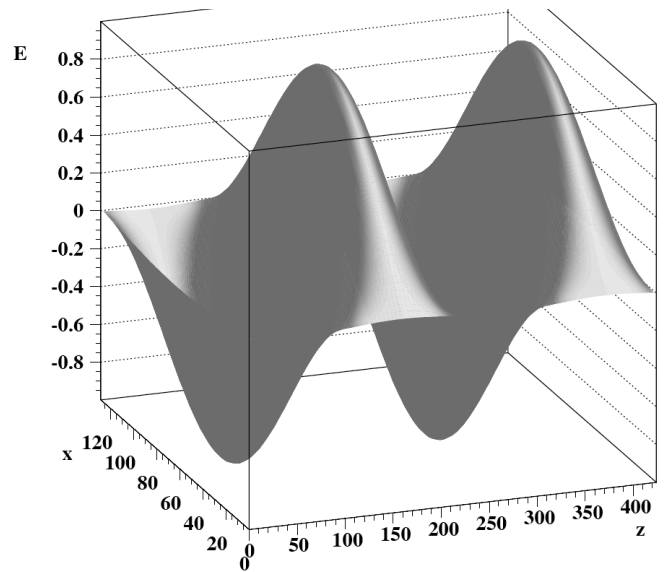
*Note: the resonant frequency is slightly reduced when the Petri dishes are inserted, due to the high conductivity of the medium.*

# Electric field

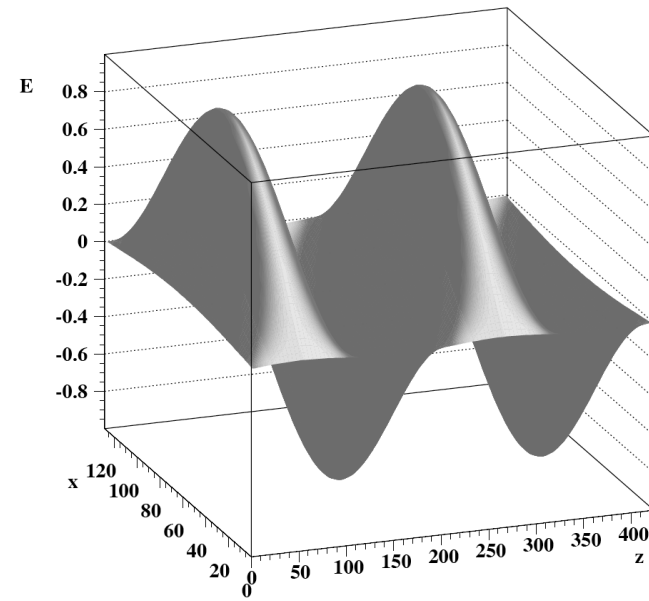


$t=0$

*The  $E$  field oscillates with time with frequency  $\nu$ , inverting the direction every half a cycle.*



$t=T/2=$   
 $1/2\nu$

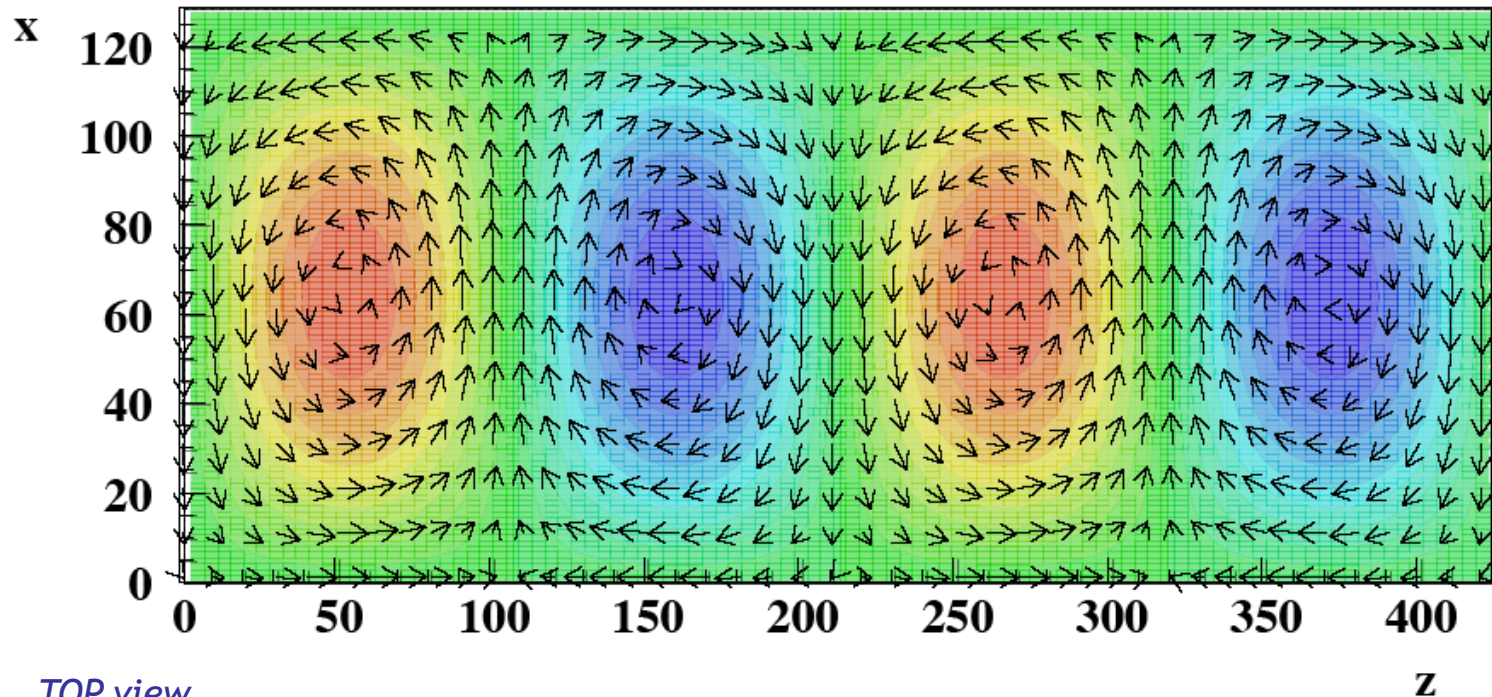


$t=T=$   
 $1/\nu$



# Magnetic field

Also the  $B$  field oscillates with time with frequency  $\nu$ , inverting the direction every half a cycle.



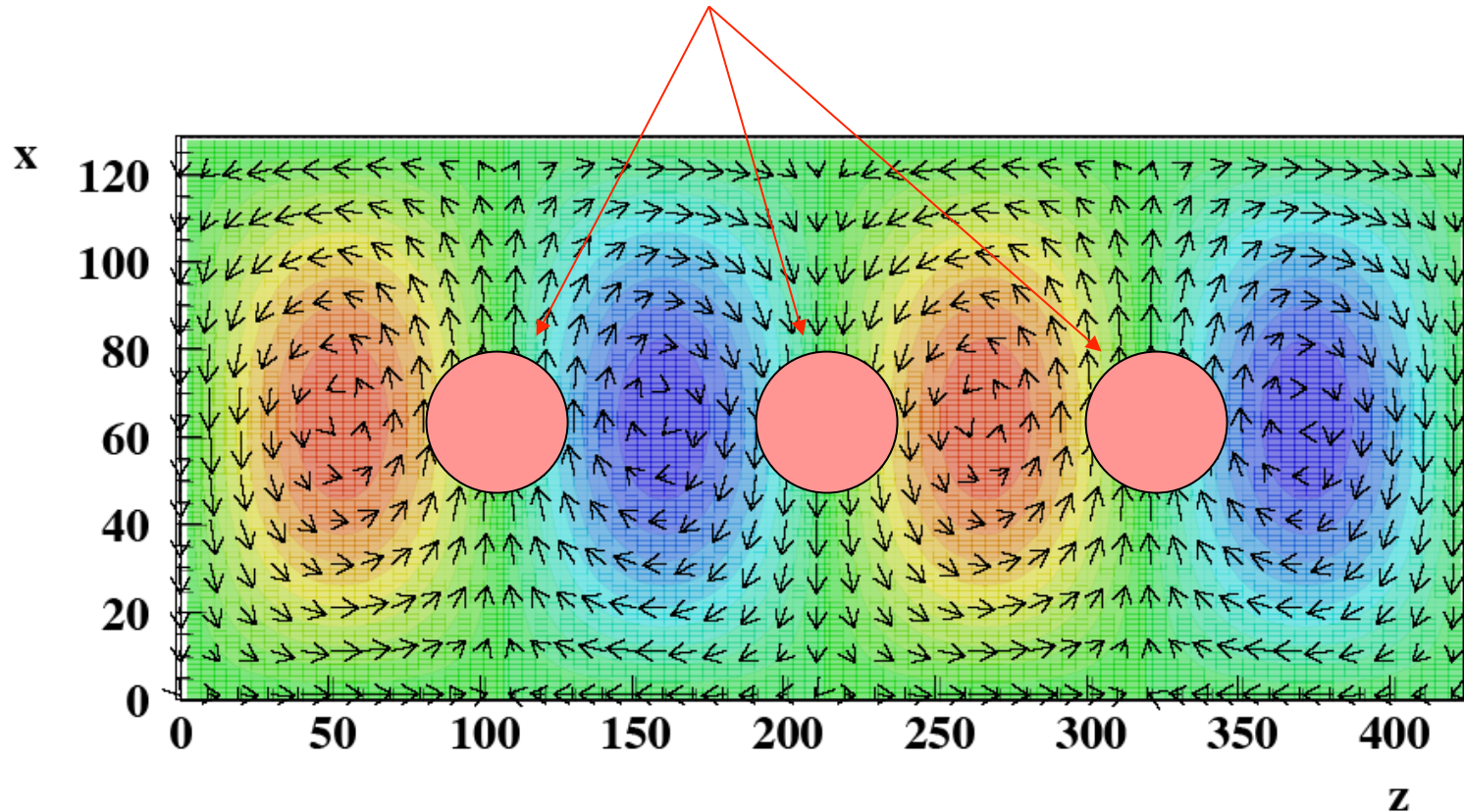
TOP view

E-field: red and blue spots

B-field: arrows

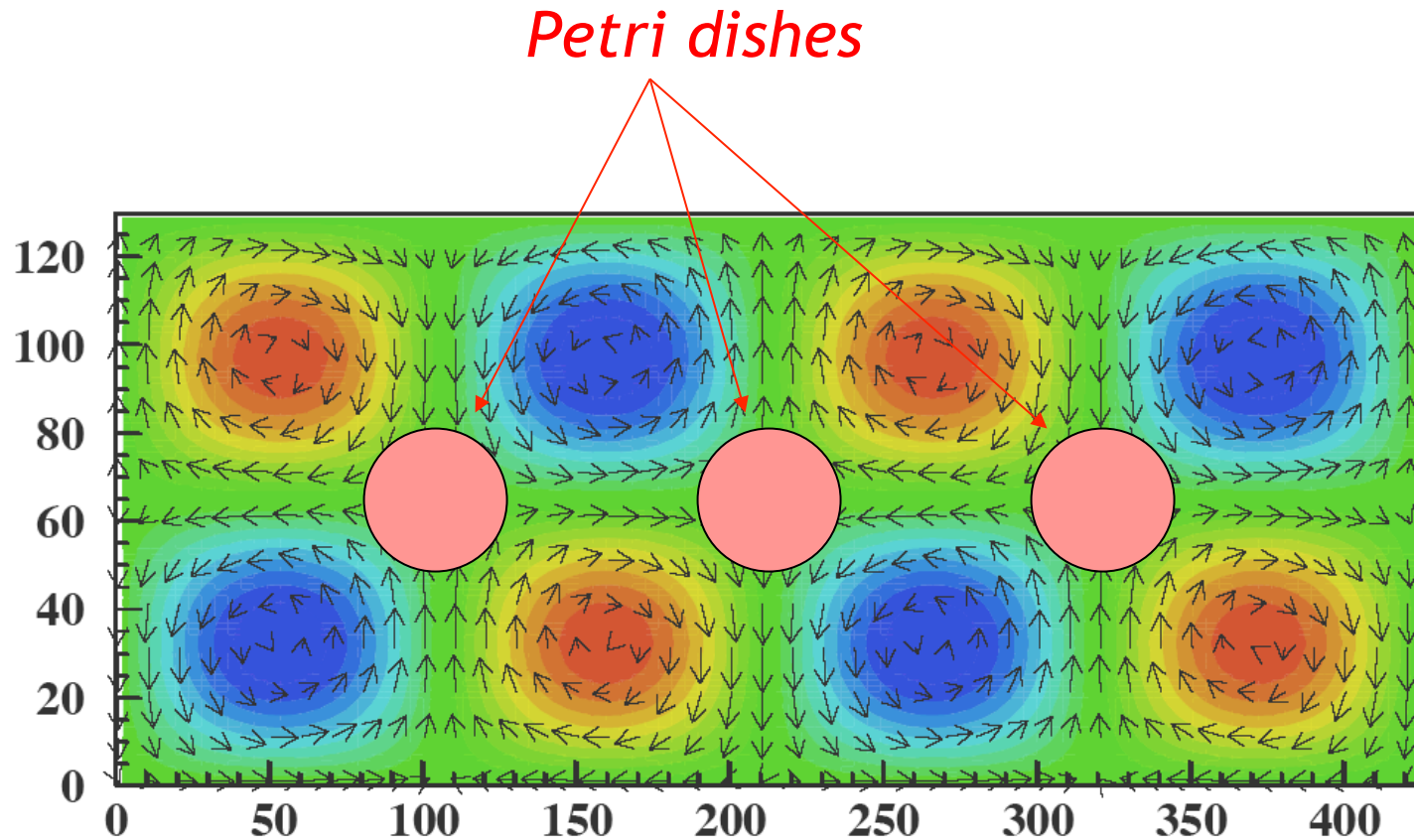
# Field on Petri dishes

*Petri dishes*

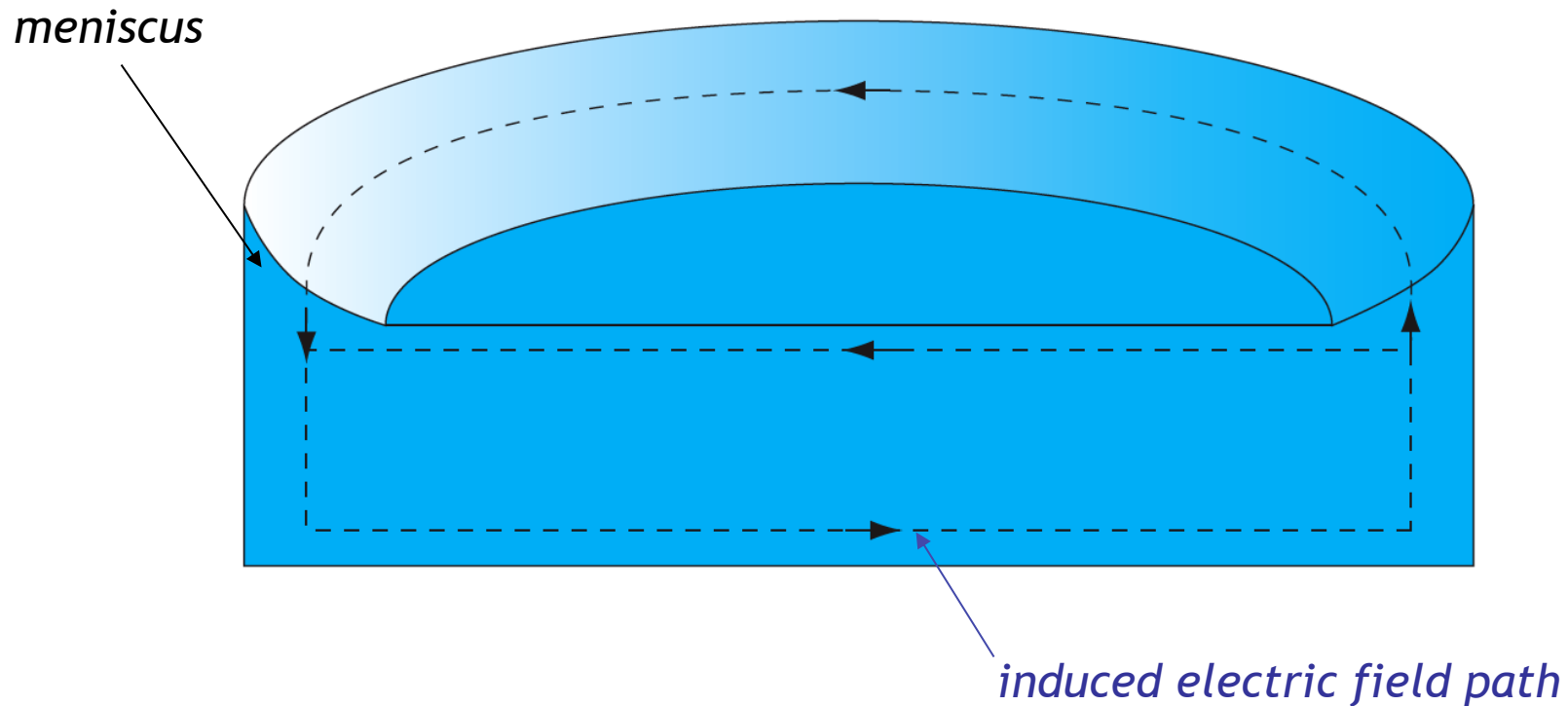


*Petri dishes are positioned where the magnetic field is larger ( $E$  is smaller).  
The magnetic field is tangent to the liquid surface.*

# *Field on Petri dishes if $n_a=2$ (resonance at 2.71 GHz)*

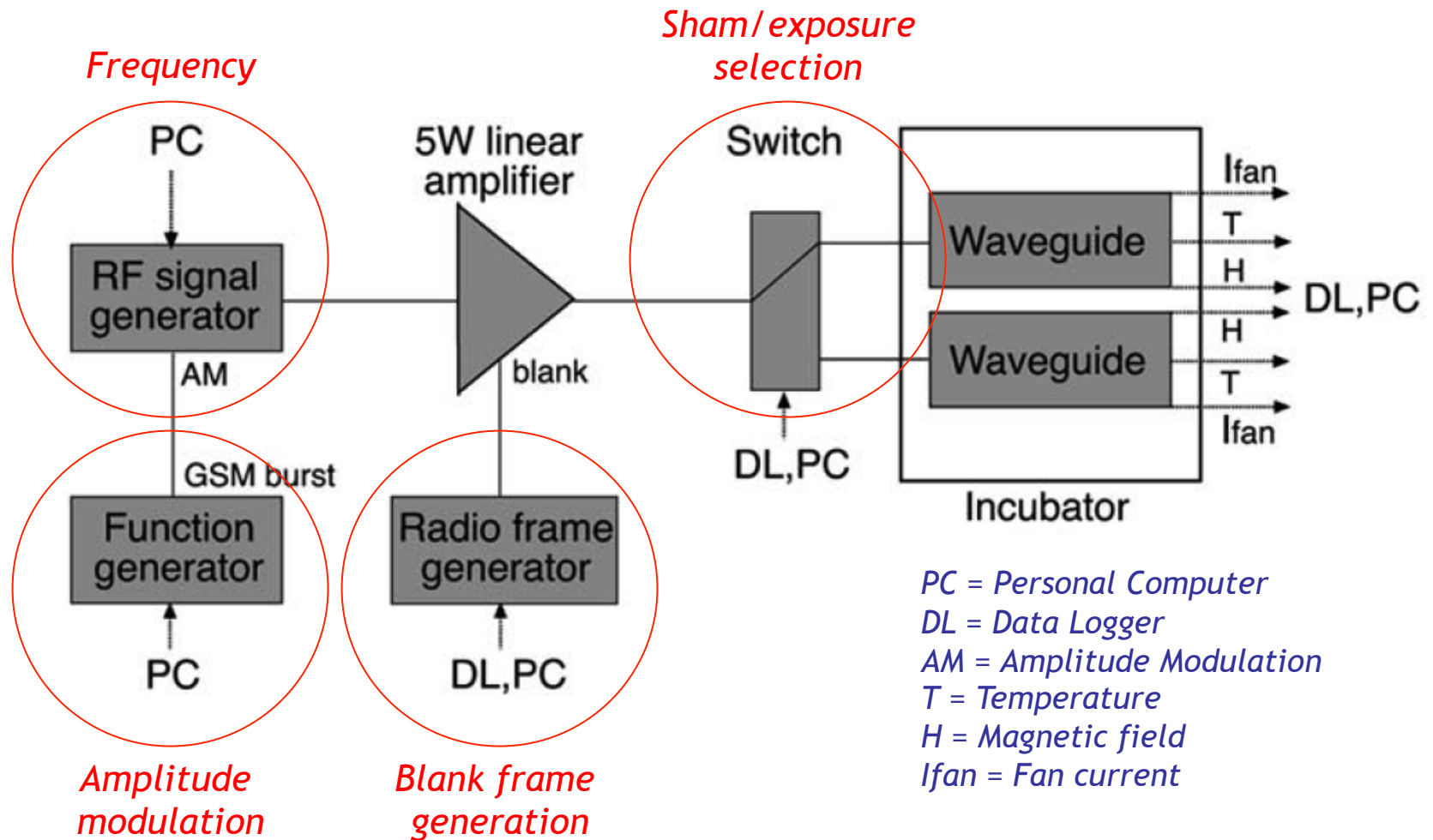


# *Induced electric field*



*Due to the large conductivity of the medium, a large oscillating electric field, circulating around the magnetic field, is induced in the liquid inside the Petri dish. The meniscus contributes with additional closed paths, further increasing the electric field.*

# Signal generation



# SAR calculation

$$\text{SAR} = \left[ \frac{\text{W}}{\text{kg}} \right] = \left[ \frac{\text{J}}{\text{kg s}} \right] = \left[ \frac{\text{Energy}}{\text{kg s}} \right]$$

## Notes:

for  $V = 3 \text{ ml}$  ( $h = 3.42 \text{ mm}$ ), the weight of the medium is:  $\rho V = \rho \pi r^2 h \approx 30 \text{ g}$   
in order to get a SAR of  $2 \text{ W/kg}$  in 1 hour, an energy of about  $22 \text{ J}$  has to be delivered  
this implies an increase in temperature of  $\Delta T = \text{Energy}/mc_v \approx 1.7 \text{ }^\circ\text{C}$  and therefore the need for ventilation

the fields can be derived from the Poynting's vector (energy/ $\text{m}^2\text{s}$ ):  
 $E \approx 45 \text{ V/m}$ ,  $B = 1.5 \text{ } \mu\text{T}$ ,  $H = B/\mu_0 \approx 1.2 \text{ A/m}$

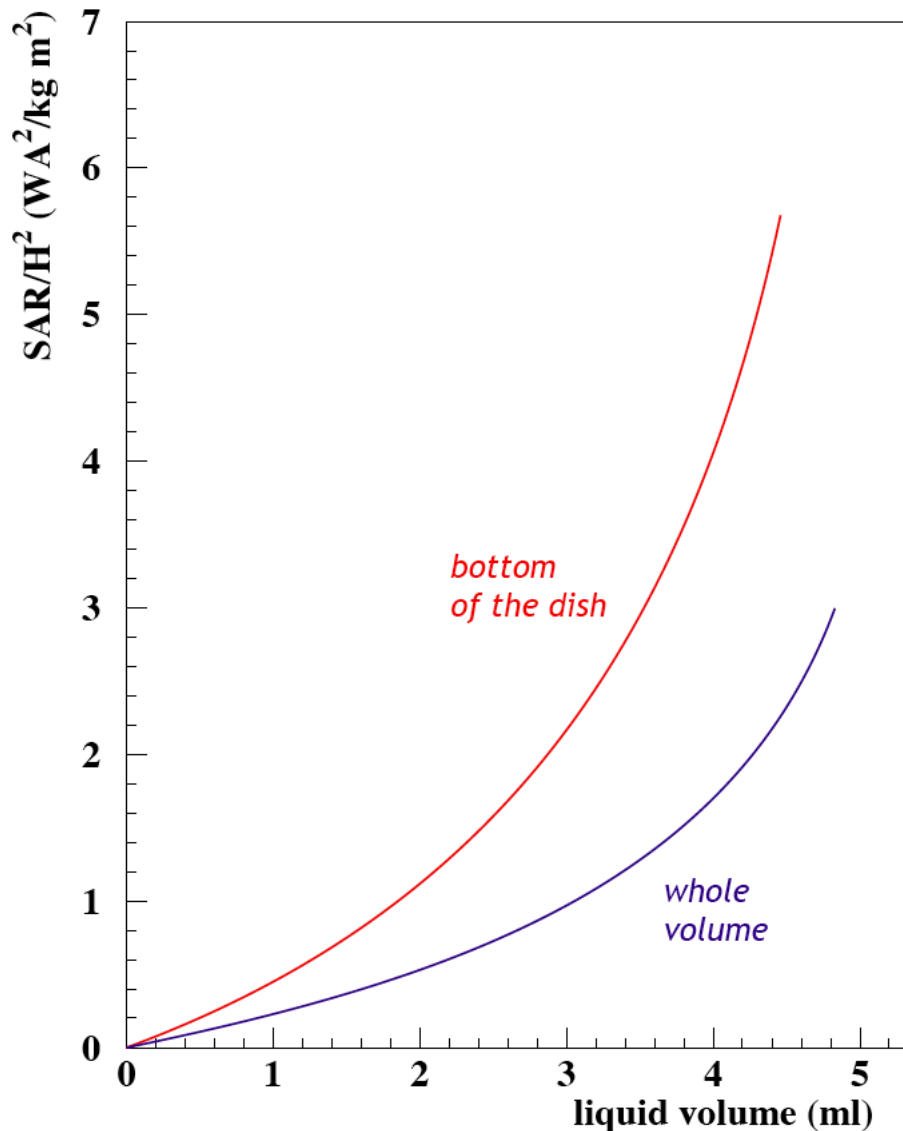
## *SAR depends on:*

- *value of the magnetic field*
- *quantity of medium*
- *position of the cells inside the medium*
- *conductivity of the medium*
- *height of the meniscus*

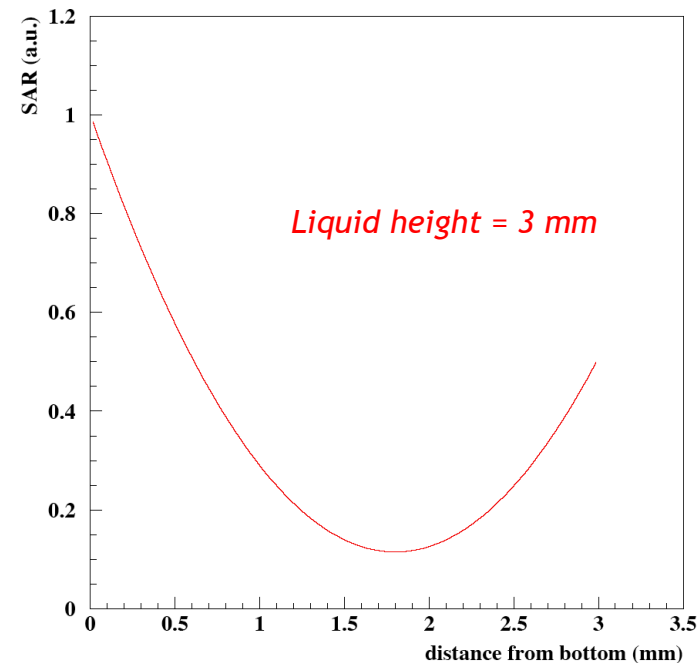
*Most results from J. Schuderer et al., IEEE Transactions on Microwave Theory and Techniques, 2004, 52:8:2057-2066.*



# *Magnetic field, medium quantity and position of the cells*



*SAR depends quadratically on the magnetic field (amplitude of the wave) and nearly quadratically on the volume of the medium.  
SAR at the bottom of the dish is largest.*





# Conductivity

*SAR depends linearly on the conductivity of the medium.*

$$SAR \approx \frac{\sigma}{\rho} |E_{\text{ind}}|^2$$

$\sigma$  = conductivity

$\rho$  = density

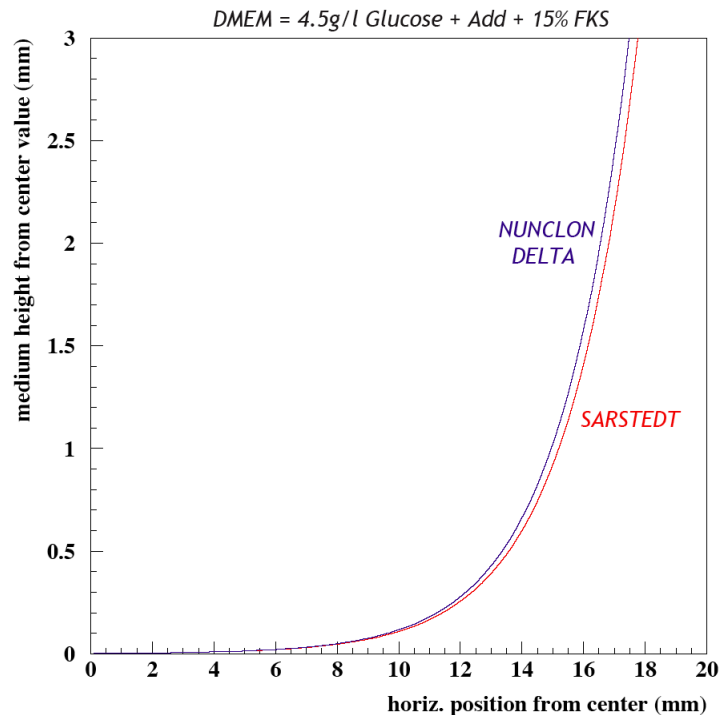
$E_{\text{ind}}$  = induced electric field

*The conductivity of different liquids may differ by 10-15%.*

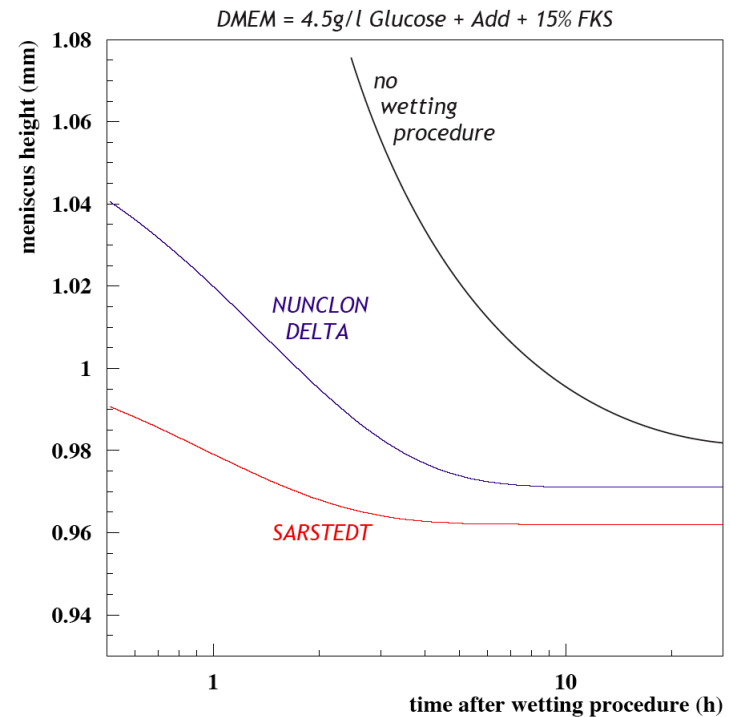
$\sigma$  (Bologna-DMEM) = 2.2 S/m

# Meniscus in different Petri dishes

## meniscus height

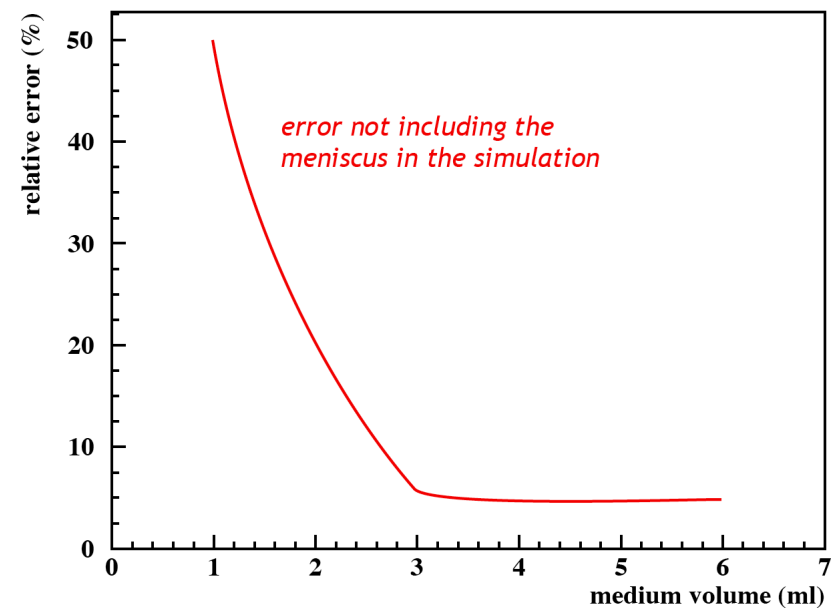
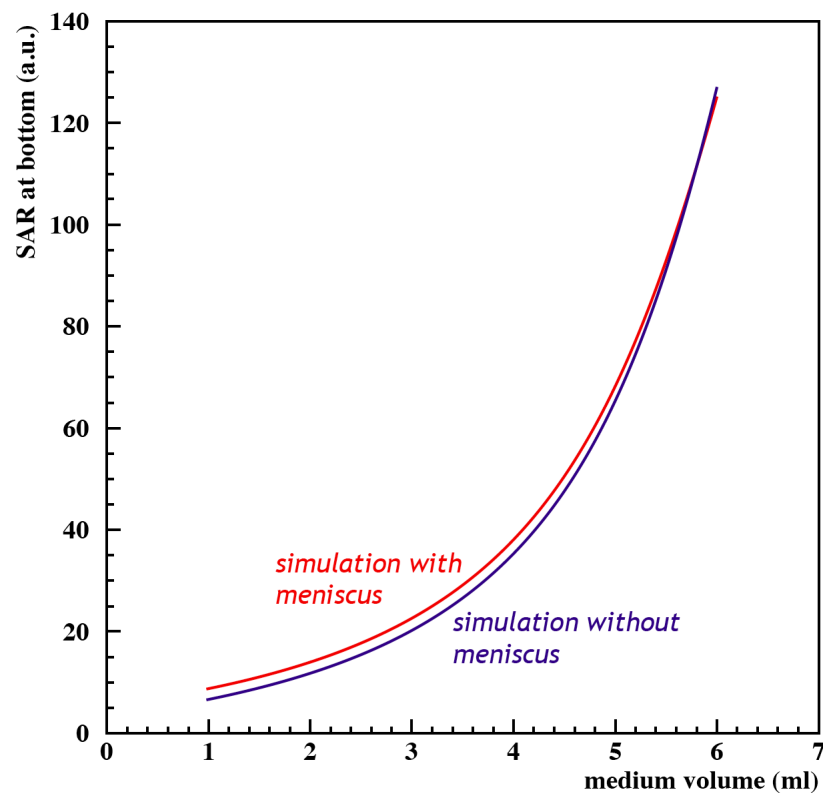


wetting procedure:  
fill with 1 ml more  
than take it away



# Meniscus relevance

*the relevance of the meniscus increases for small volumes*



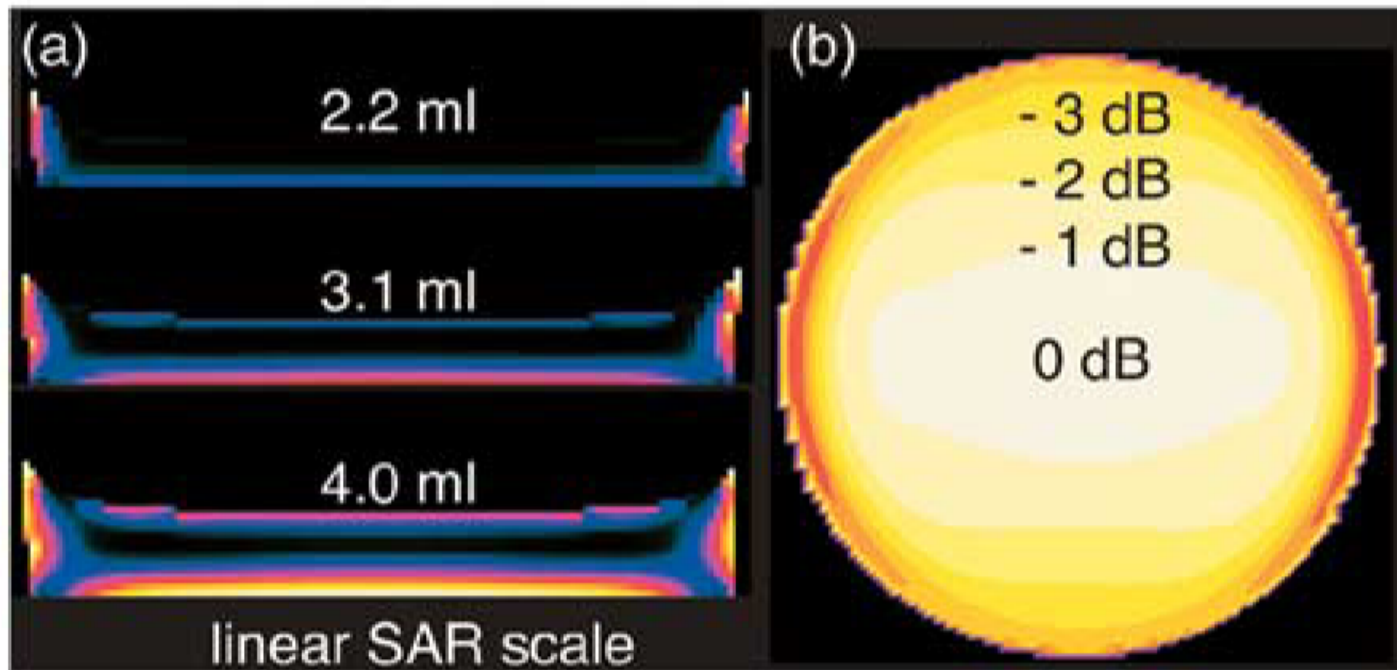
## *Uncertainty of SAR assessment (experimental)*

Fit for extrapolation to monolayer	2.8%
Fit for varying medium volume (2.2 - 4.9 mL)	1.9%
Height of cell monolayer ( $z \leq 0.1$ mm)	4.8%
Numerical discretization ( $0.1 \text{ mm}^3$ reference)	8.2%
Determination of medium volume ( $\pm 5 \mu\text{L}$ )	0.3%
Determination of dielectric parameters	11%
Calibration of dosimetric E-field probe	7.6%
Probe positioning in Petri dish	1.6%
Calibration of monopole sensor for incident fields	11%
<i>Combined relative uncertainty (RSS)</i>	<b>20%</b>

## *SAR variability*

Frequency dependency of loop coupler	4.5%
Determination of medium volume ( $\pm 5\mu L$ )	0.3%
Dish holder misplacement in waveguide ( $\pm 2mm$ )	0.7%
Assessment of incident fields	2.2%
Power drift	0.5%
<i>Combined relative variability (RSS)</i>	<b>5.1%</b>

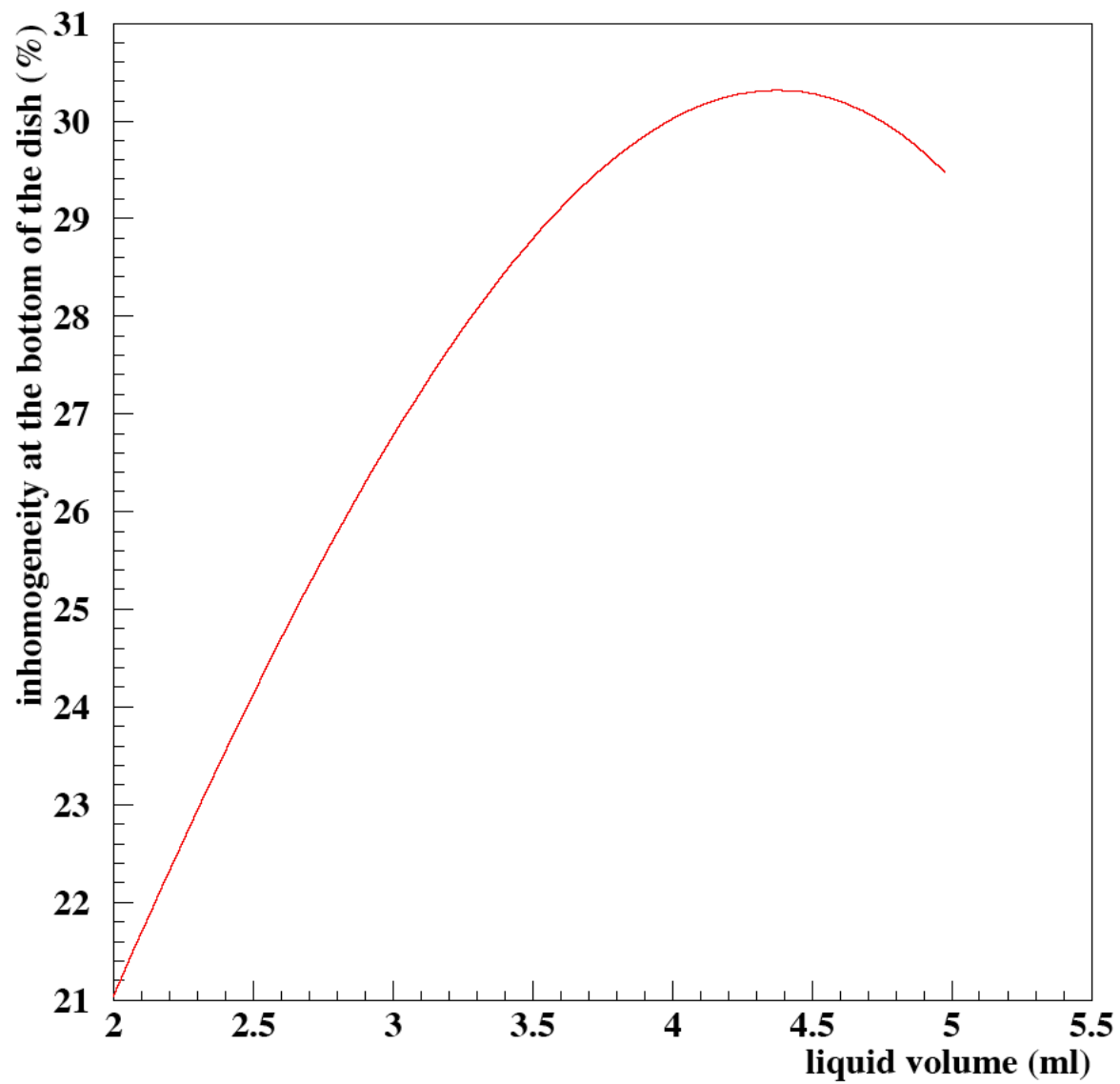
## *SAR inhomogeneity: simulation results*



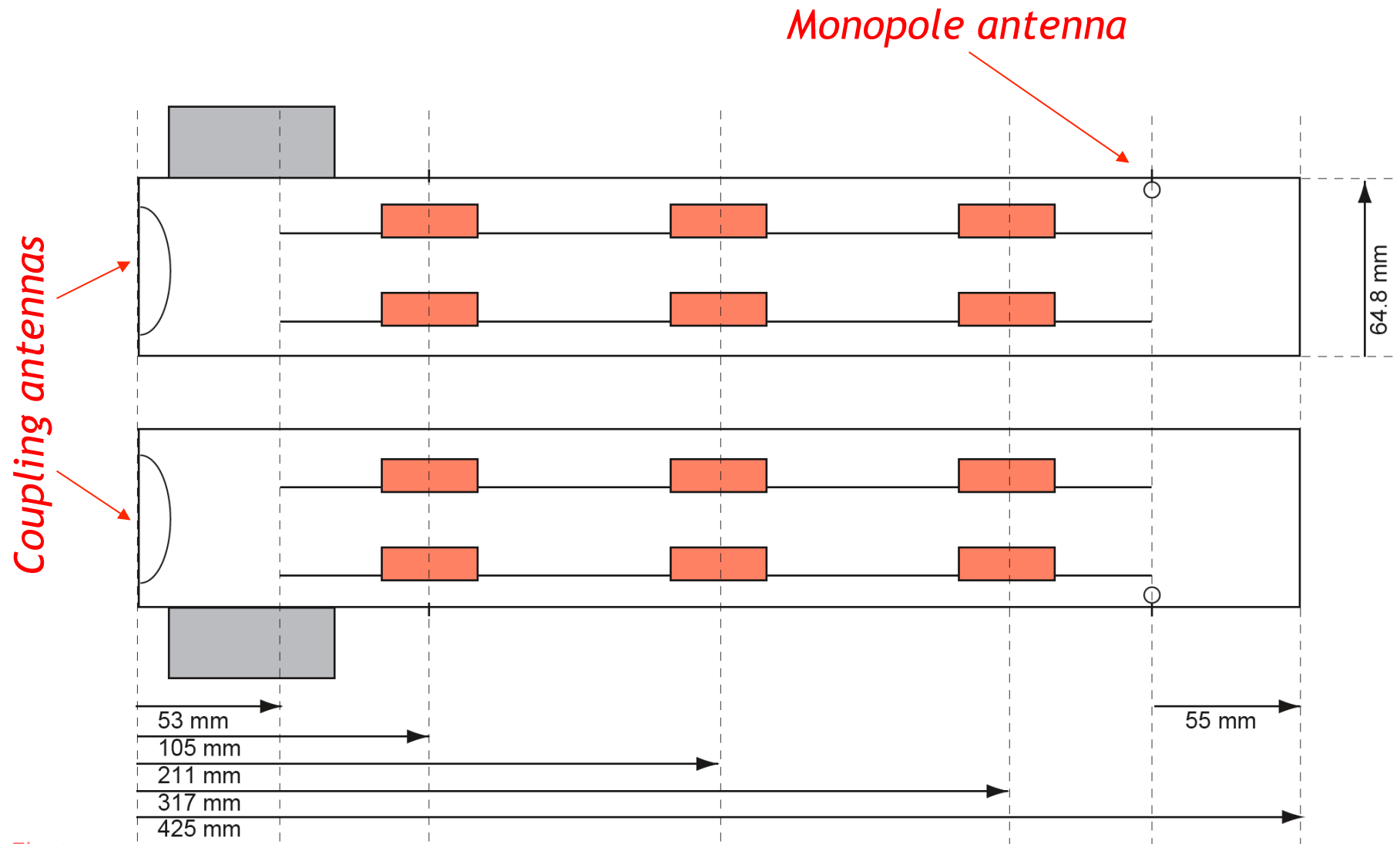
*Side view*

*Top view*

# *SAR inhomogeneity*



# Measurement of the magnetic field





# Summary

*The dosimetric quantity has been parametrized w.r.t. the relevant parameters:*

$$\text{SAR}_{\text{bottom}} = (1.90 - 1.26h + 0.39h^2)H^2$$

$$\text{SAR}_{\text{bottom}} = (2.60 - 1.84V + 0.49V^2)H^2$$

$$\text{SAR}_{\text{medium}} = 0.11 + 0.39 \text{SAR}_{\text{bottom}}$$

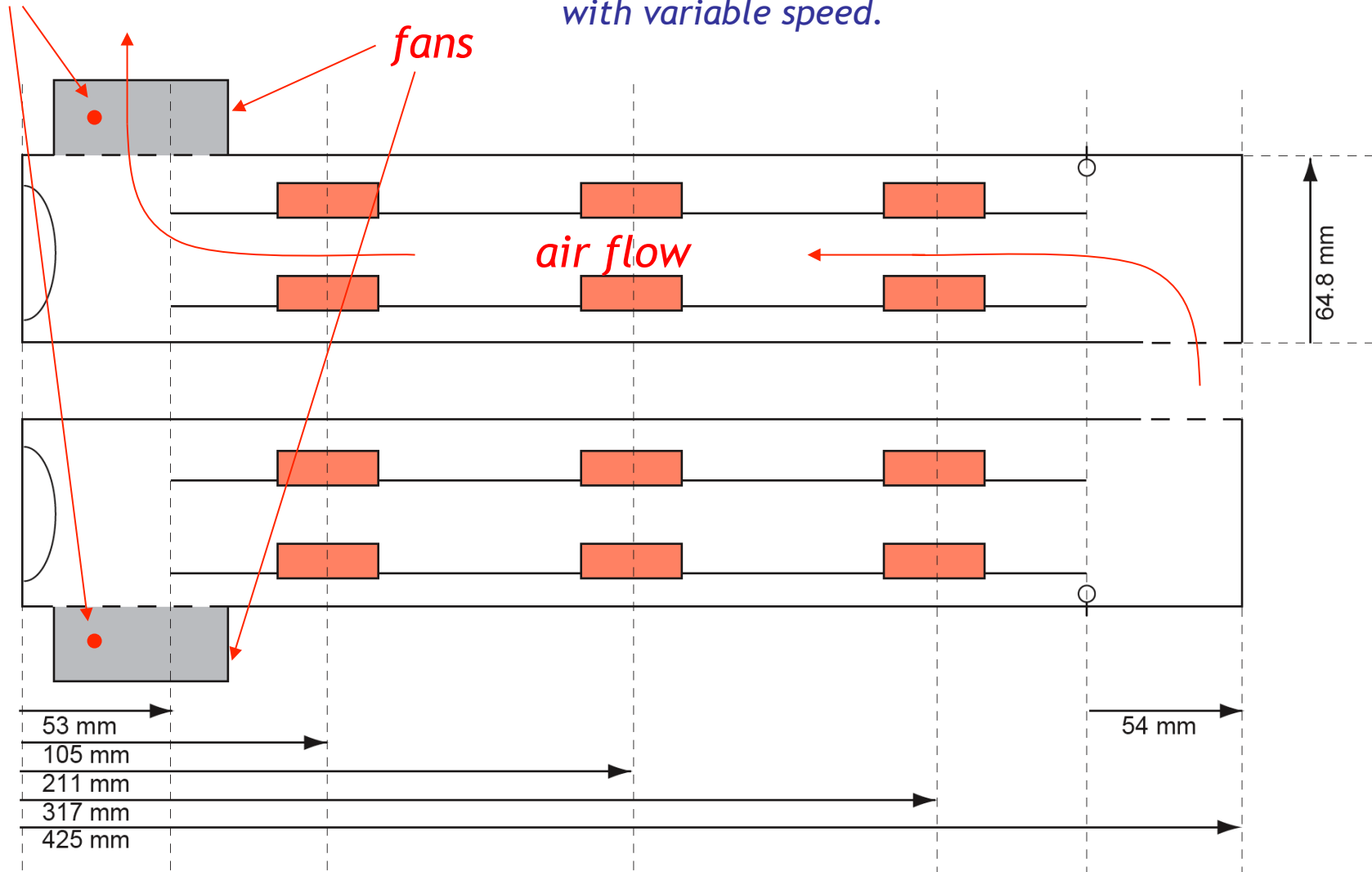
$$\frac{\sigma_{\text{SAR}}}{\text{SAR}} = 7.70 + 5.94V + 0.83V^2 - 0.23V^3$$

*Note: the parameters of the fits are dependent on the geometry of the device.*

# Temperature control

*thermometers*

*The temperature stability is guaranteed by fans with variable speed.*



# Temperature variation due to the EM field

$$\frac{dT_{\text{medium}}}{dt} = -\frac{T_{\text{medium}} - T_{\text{incub}}}{\tau} + \frac{\text{SAR}_{\text{medium}}}{c_w}$$

$\tau$  = heat convection time constant (180 s)

$c_w$  = water specific heat

ON CYCLE:  $T(t) = T_{\text{incub}} + \tau_{\text{on}} \frac{\text{SAR}_{\text{medium}}}{c_w} - \tau_{\text{on}} \frac{\text{SAR}_{\text{medium}}}{c_w} e^{-\frac{t}{\tau_{\text{on}}}}$

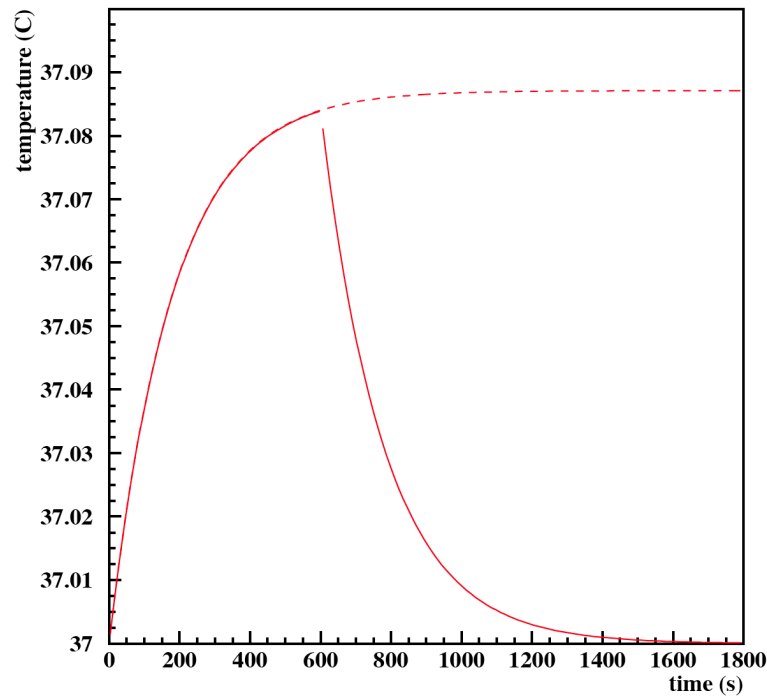
OFF CYCLE:  $T(t) = T_{\text{incub}} + (T(t_0) - T_{\text{incub}}) e^{-\frac{t}{\tau_{\text{off}}}}$

# Temperature variation

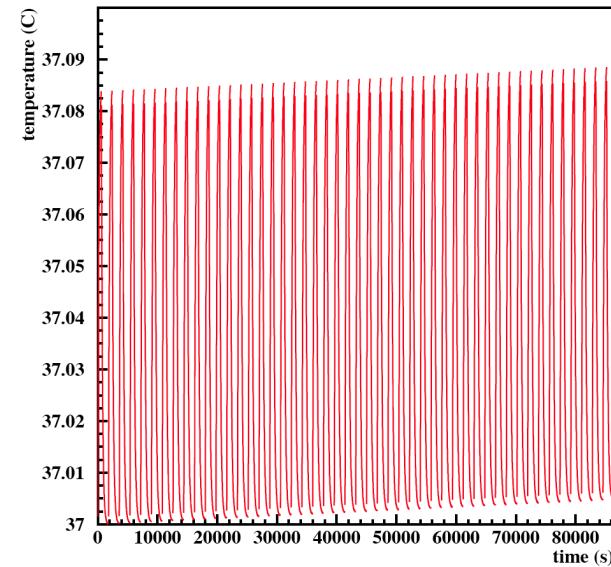
cycle: 600 s on / 1200 s off

SAR = 2 mW/g

Total duration: 24 h



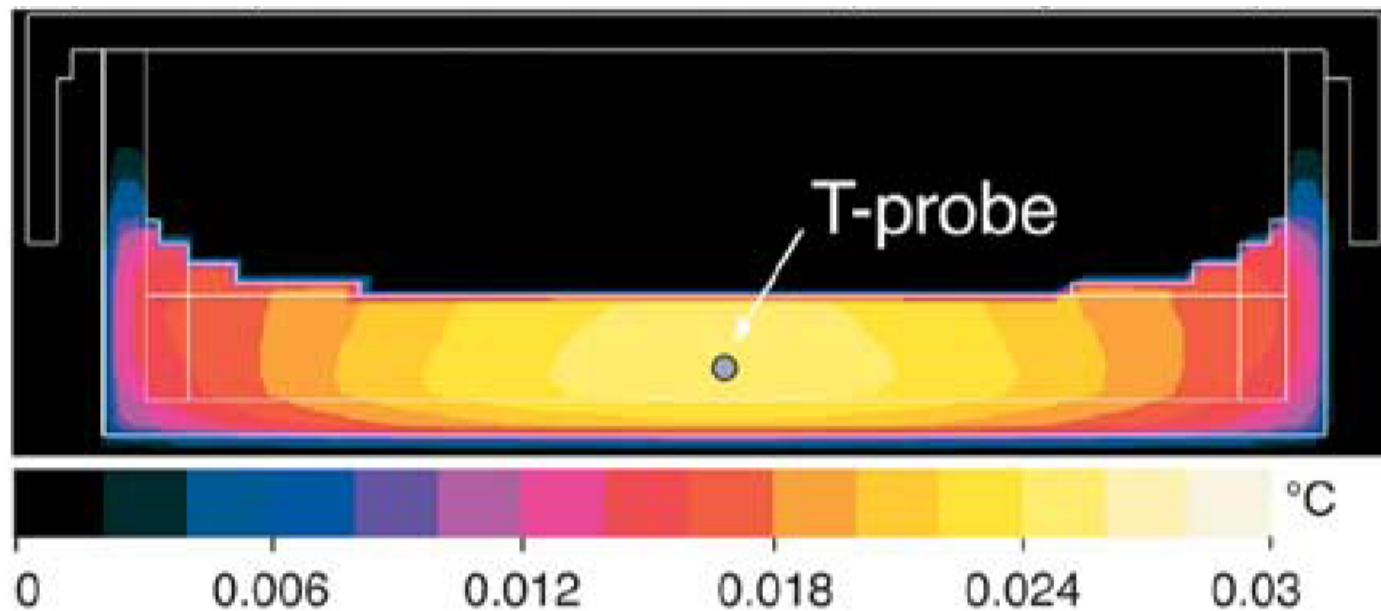
*1 cycle*



*full experiment*

# *Temperature inhomogeneity*

*SAR = 1 W/kg*



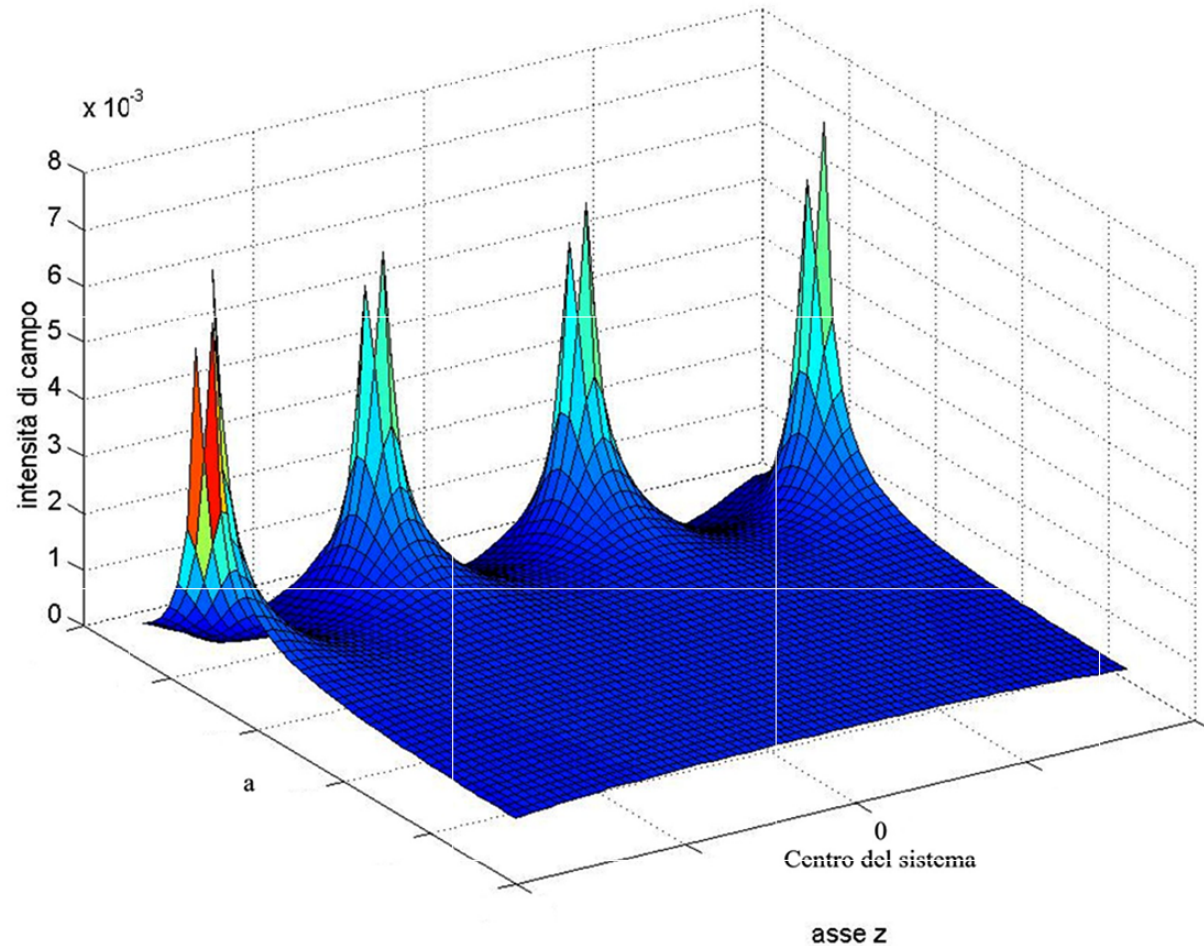
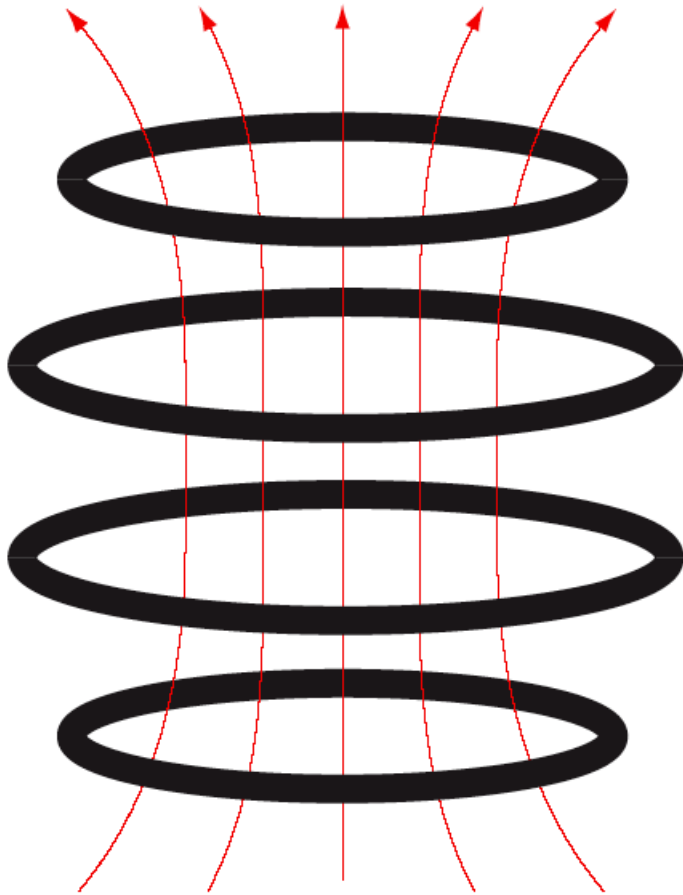
# *Low frequency irradiation*

*Because of the high conductivity of the biologic material, in the case of low frequency irradiation only the magnetic field and the currents induced by its variation are relevant.*

*The low frequency fields penetrate completely inside the body.*

# The Bologna apparatus

Solenoidal field with four coils.  
All coils are doubled to allow for  
counter-rotating currents, i.e.  
sham exposure



*Most important is the homogeneity  
of the field inside the Petri dishes*